Preface

We are thankful to Almighty ALLAH Who has given us an opportunity to write the book , named 'Applied Mathematics-I ' as Textbook, intending to cover the new syllabus for the first year students of Diploma of Associate Engineer (DAE)

Throughout the text, emphasis is on correct methods of computation, correct method for transposition of formulae, logical layout of solutions, neatness and clarity of arrangement of material and the systematic use of all the normal mathematical and other tables.

Topics covered include algebra, trigonometry, vectors & Phasors Algebra, Complex numbers, Number Systems, Boolean Algebra, Straight Line and The Circle.

Normally students face difficulty in solving complicated problems because they do not make a systematic attempt. We have attempted to help the students to overcome the difficulty by providing detailed instructions for an orderly approach. Difficult procedures and types of problems appearing in the exercise are illustrated by carefully explained examples. In the presentation of these illustrated examples, we have avoided unnecessary explanations. It is hoped that this book will help to give students a good foundation in old and new techniques.

Students are reminded that in order to acquire a proper understanding of the subject and its application, it is necessary to learn a number of sound basic rules and methods.No scientific or engineering subject can be fully comprehended and satisfactorily studied without a sound mathematical background.

We would like to express , sincere and thanks to Mr.Jawad Ahmed Qureshi Chief Operating Officer TEVTA,Engr. Mr.Azhar Iqbal Shad G.M Academic,Engr.Mazhar Abbas Naqvi Manager (Curriculum) and Engr. Syed Muhammad Waqar ud- Din Deputy Director(technical) Curriculum Section Acade mics Wing, who took keen interest and inspired us for the completion of this task.

We made every effort to make the book valuable both for students and teachers , however we shall gratefully welcome to receive any suggestion for the further improvement of the book.

Authors.

A Textbook of

APPLIED
MATHEMATICS-I

Math–123

For

First year
Diploma of Associate Engineer
(DAE)

Including:
Objective Type
and
Short Questions

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